

Thermophoresis of charged colloidal spheres and rods

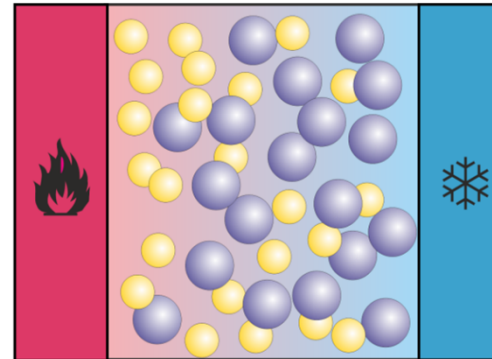
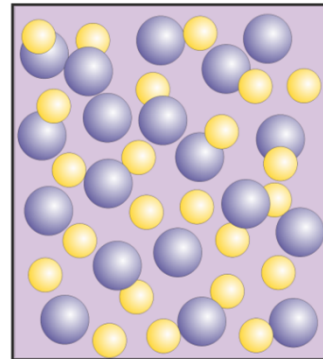
20. Mai 2015

| Simone Wiegand, Dzmitry Afanasenkau, Olga Syshchyk, Zilin Wang,
Johan Buitenhuis and Jan K.G. Dhont

Phenomenological equation

(..., thermodiffusion, Soret effect) –

Movement of particles driven by a temperature gradient



D - diffusion coefficient,

c - concentration,

D_T - thermodiffusion coefficient,

\vec{j} - flux, T – temperature

S_T – Soret coefficient

$$\vec{j} = -D\vec{\nabla}c - c(1-c)D_T\vec{\nabla}T$$

Steady state $\vec{j}=0$

$$S_T = \frac{D_T}{D} \propto \frac{\Delta c}{\Delta T}$$

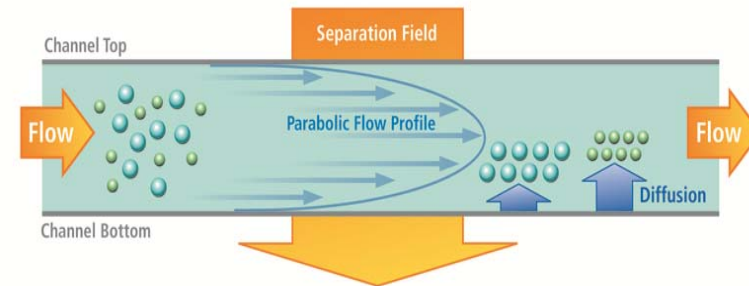
Thermophoresis: What ? Where is it used?

Application areas

- Characterization of macromolecules and colloids, e.g. TFFF (thermal field flow fractionation)
- Separation of mixtures, e.g. thermogravitational column
- **Measuring equilibration constants of biochemical reactions**
- **Studying interaction and folding of macromolecules**

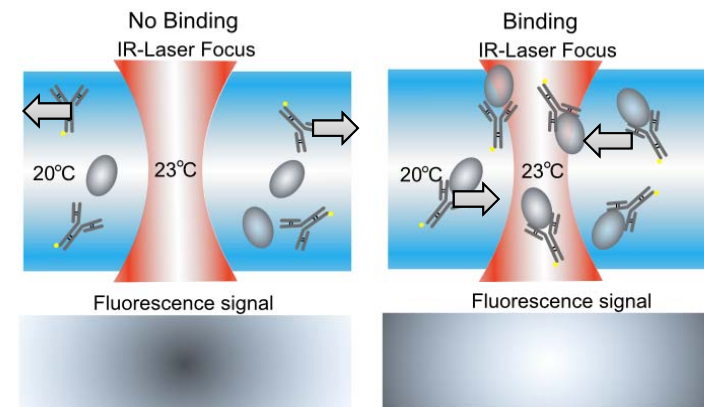
Application examples

- Thermal field flow fractionation



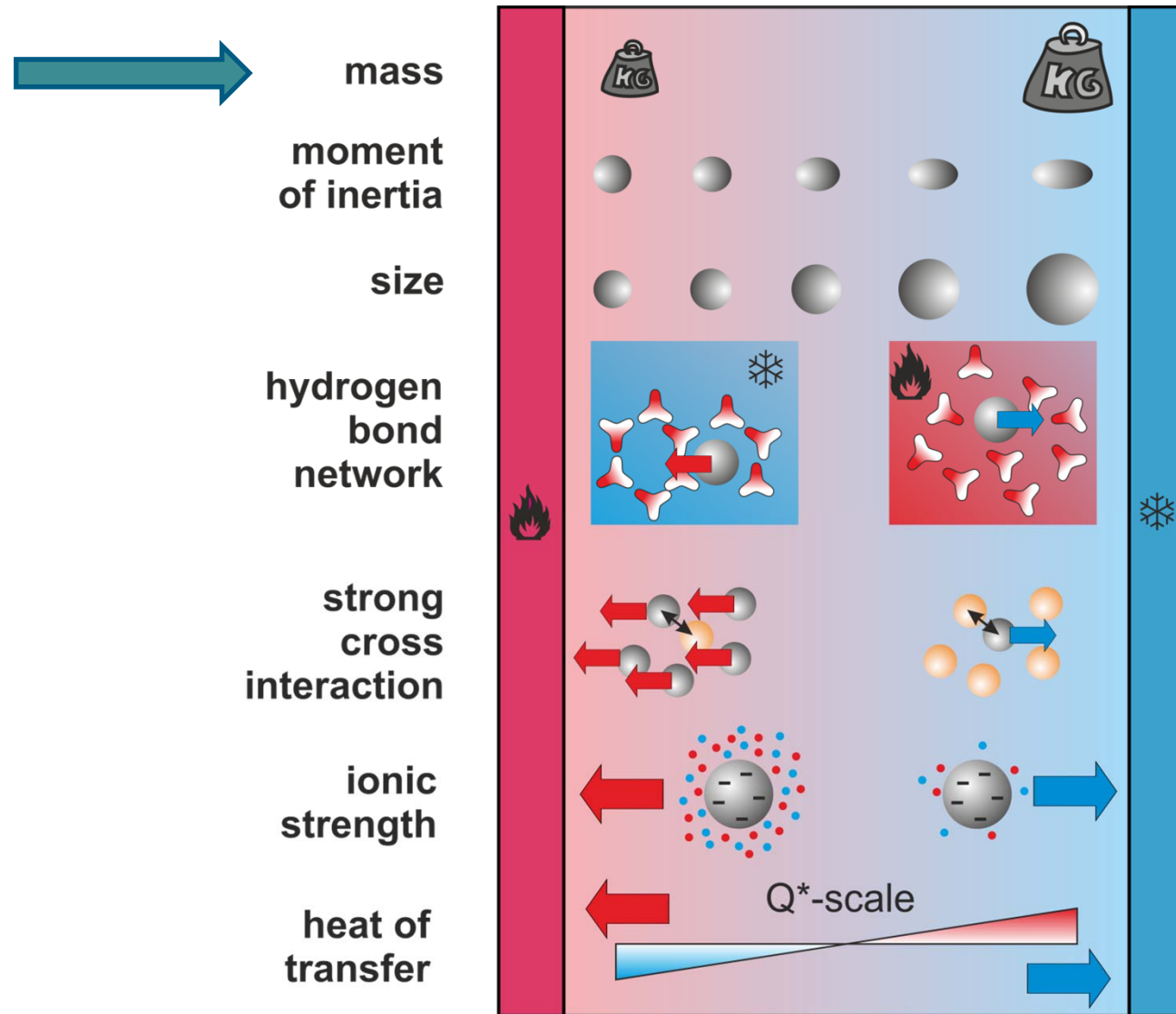
Separation of mixtures (TFFF) //Wikipedia

- Microscale thermophoresis



**Microscale Thermophoresis:
Technology and Applications**
//NanoTemper GmbH

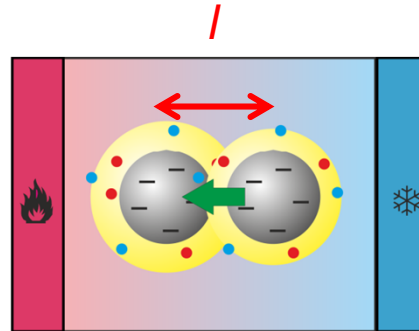
To the warm or to the cold?



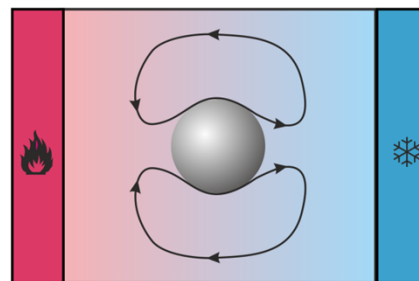
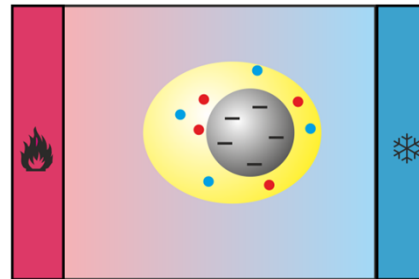
Influence of charges

$$\lambda_{\text{DH}} \propto \sqrt{\frac{T}{I}}$$

T .. temperature
 I .. ionic strength



... of minor importance in water, but relevant in solvents with low dielectric constant



$$\delta W^{rev} = - \int \cdot F_{\text{tot}}$$

internal force F_w due to change of the double layer structure on displacement of the sphere

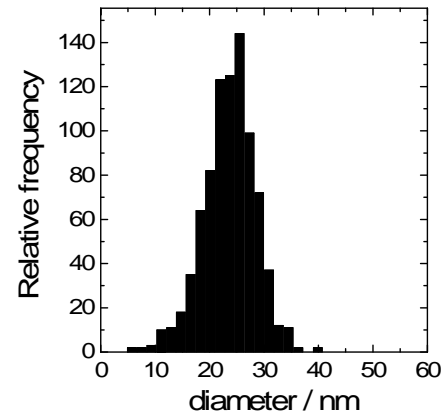
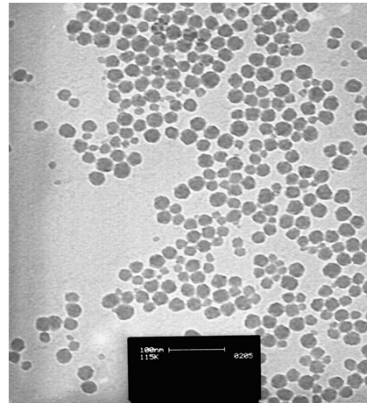
electric force F_{el} due to non-spherical symmetry of the double layer structure.

solvent-friction force F_{sol} due to solvent flow arising from the asymmetry of the double-layer structure.

[J. K. G. Dhont and W. J. Briels, Eur. Phys. J. E **25** (2008) 61-76]

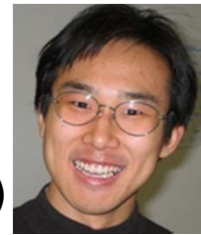
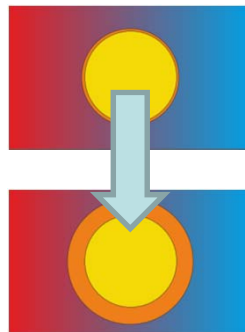
Ionic strength effect

charged silica colloidal particles (Ludox)



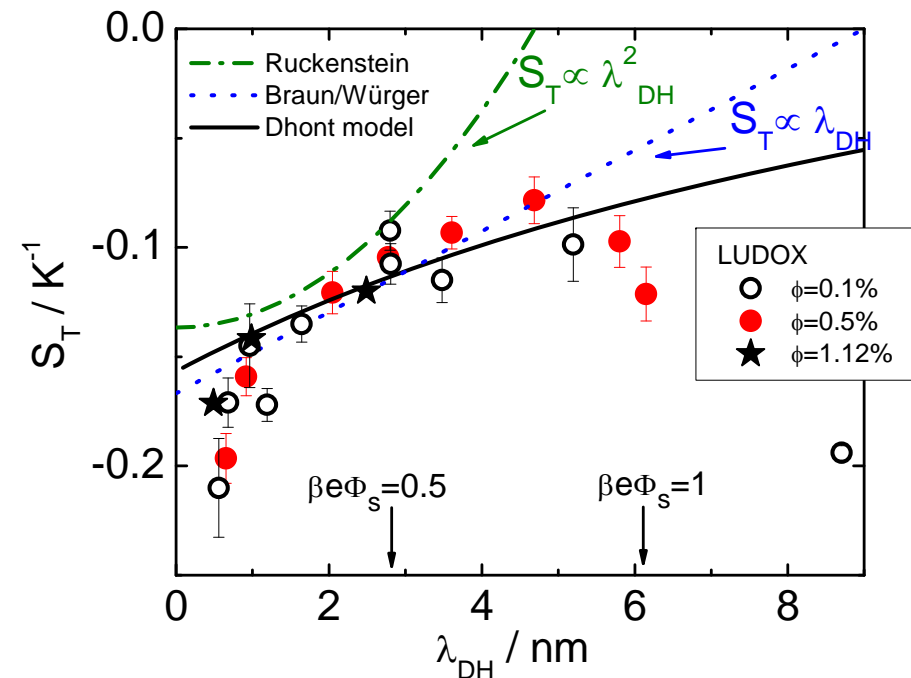
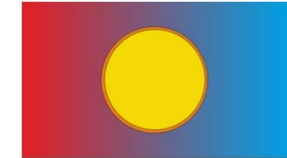
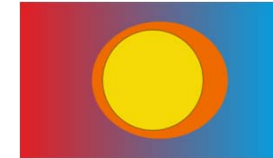
valid for thin and thick double layers:

e ... elementary charge
 l_B .. Bjerrum length
 σ .. surface charge density
 $\kappa^{-1} = \lambda_{DH}$.. Debye length
 ϵ .. dielectric constant
 a .. radius of the colloid



Hui Ning

E. Ruckenstein, J. Colloid Interface Sci. 83, 77 (1981)
 S. Fayolle et al., Phys. Rev. Lett. 95, 208301 (2005)

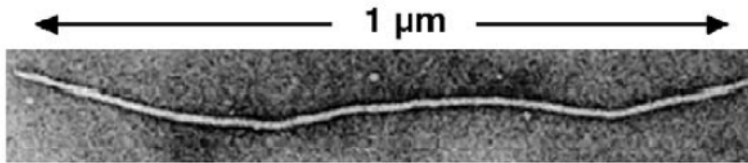


$$S_T = \frac{1}{T} \left\{ 1 + \frac{1}{4} \left(\frac{4\pi l_B^2 \sigma}{e} \right)^2 \frac{1}{(1 + \kappa a)^2} \frac{\kappa a^4}{l_B^3} \left\{ 1 - \frac{d \ln \epsilon}{d \ln T} \left(1 + \frac{2}{\kappa a} \right) \right\} \right\} + A(T)$$

[H.Ning, J.K.G. Dhont, SW, Langmuir, 24 (2008), 2426]
 [Dhont, J. K. G.; SW; Duhr, S.; Braun, D. Langmuir, 23 (2007), 1674]

Model system for a charged rod: fd-virus

System: *wt* fd-virus

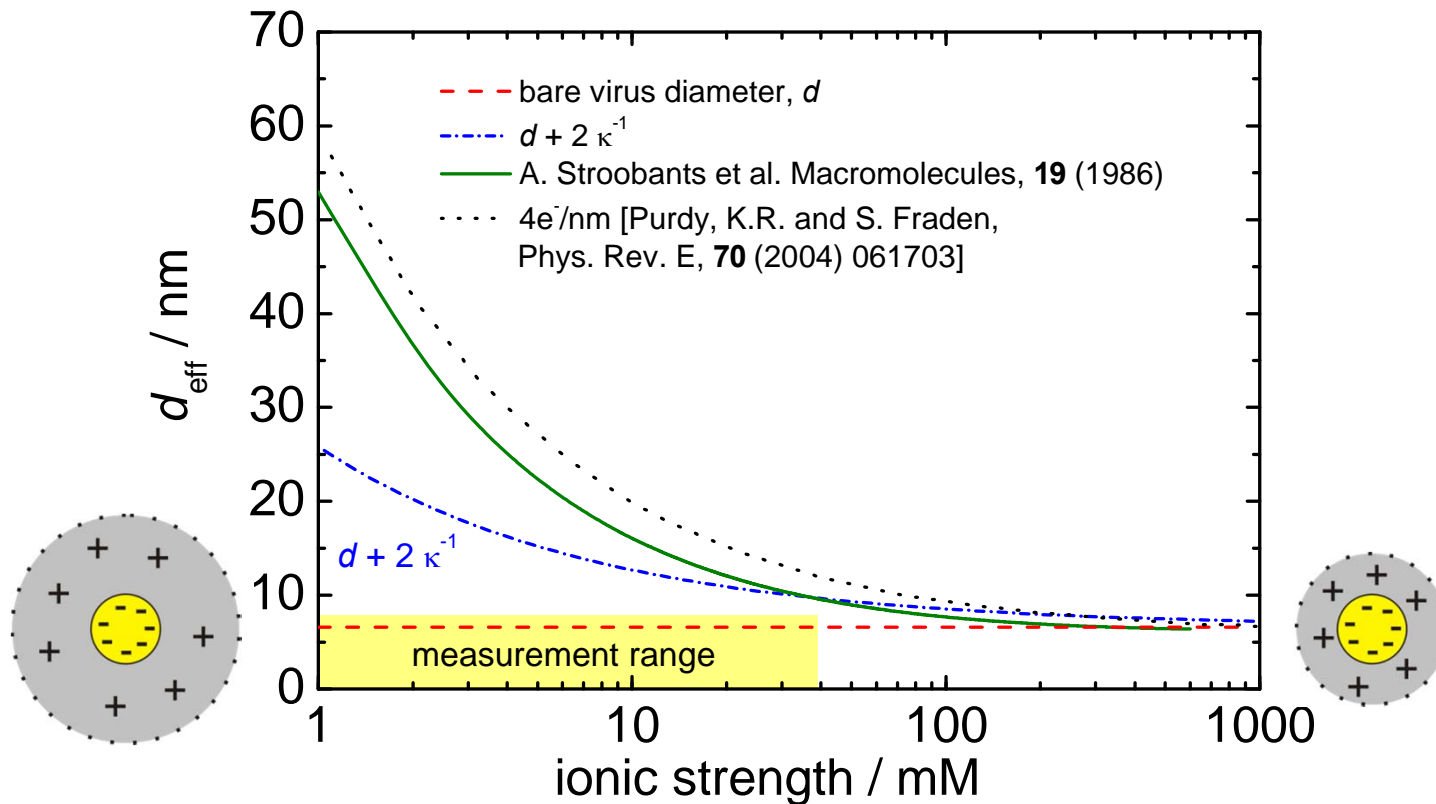


Diameter = 6.6 nm

Length = 880 nm

Molar mass = 1.64×10^7 g/mol

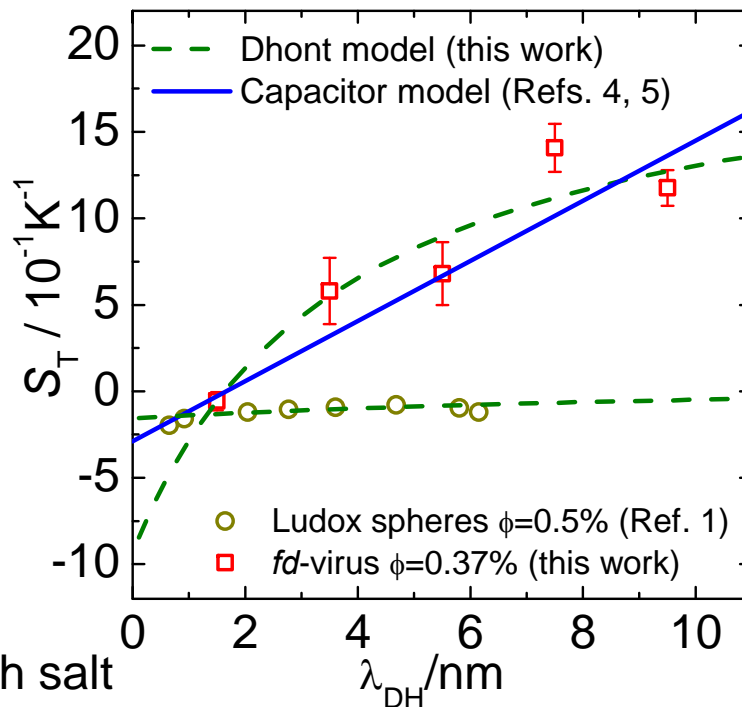
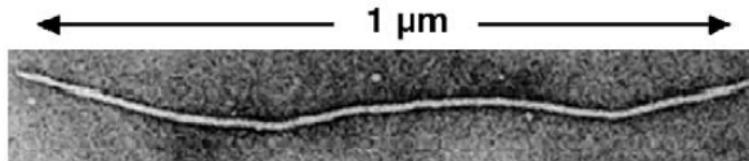
Effective diameter



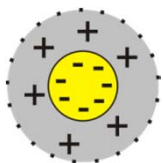
Onsager, L., *Ann. N.Y. Acad. Sci.*, **51**(1949) 627-659.

Single particle effects: charged colloidal rod

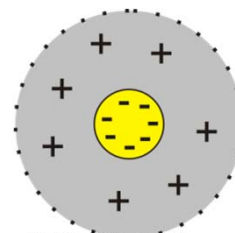
System: wt fd-virus



high salt

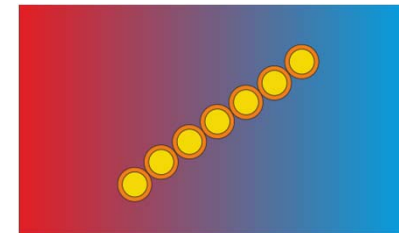


low salt

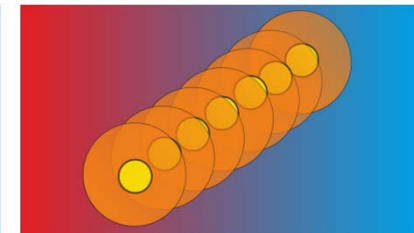


Theoretical description

Thin double layer



Thick double layer



Model	σ/enm^{-2}	Offset
Dhont	0.050 ± 0.003	-1.39
Capacitor	0.016 ± 0.002	-0.74
Calculated bare charge	0.066	



Zilin Wang

Folie 8

20. Mai 2015

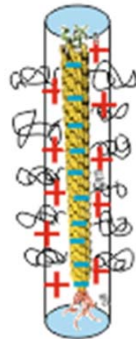
[Wang, Z., H. Kriegs, J. Buitenhuis, J.K.G. Dhont, and SW, Soft Matter, 9 (2013) p. 8697]

Charged colloidal rod with hairs



Johan Buitenhuis

Ionic strength > 20mM

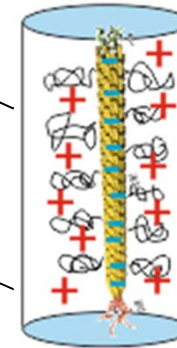


MPEG=5000g/mol

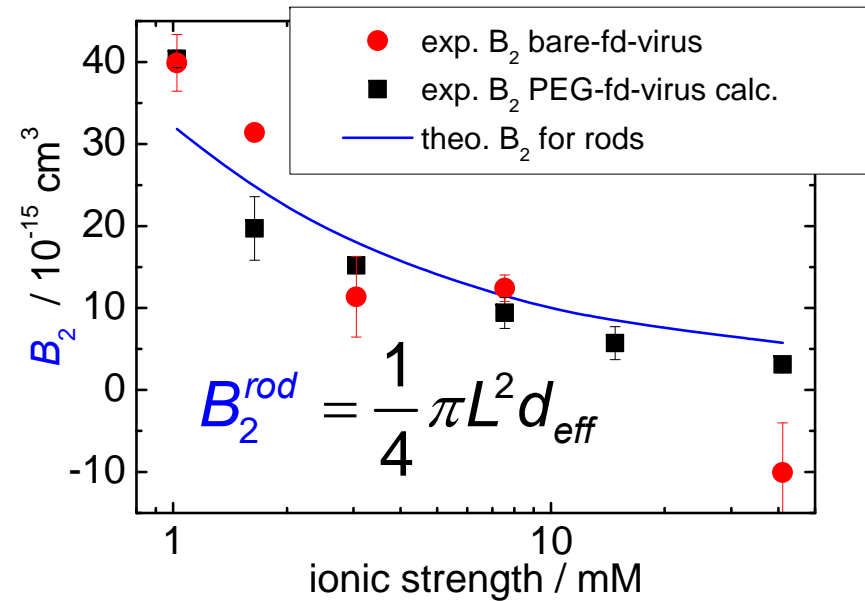
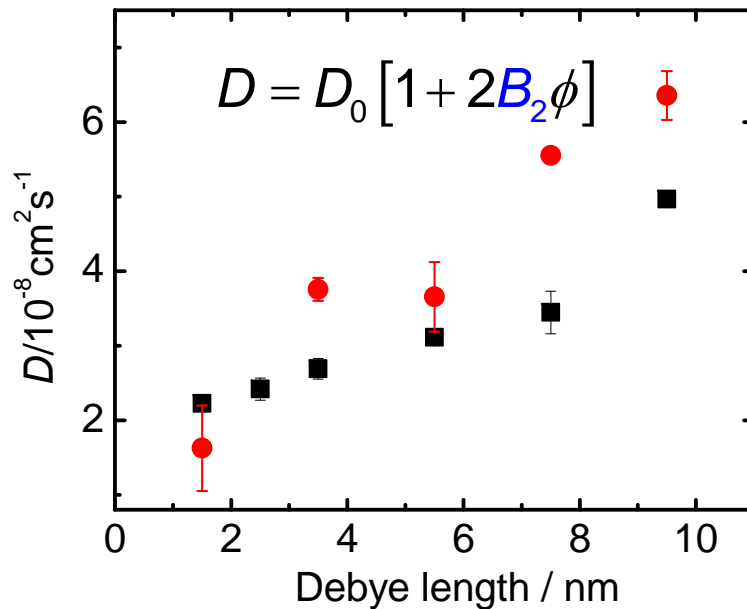
Steric vs. electric interaction

Ionic strength < 20mM

Electric double layer

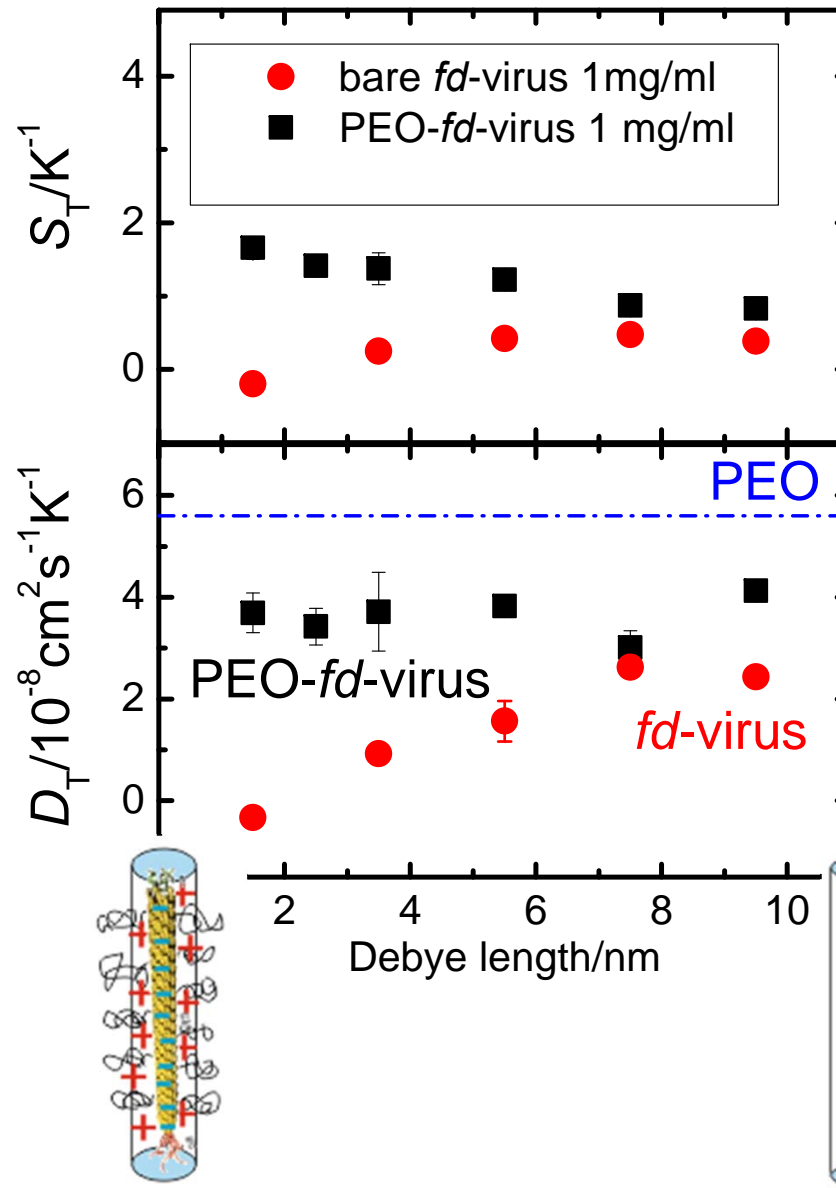


Zilin Wang



Diffusion remains almost the same

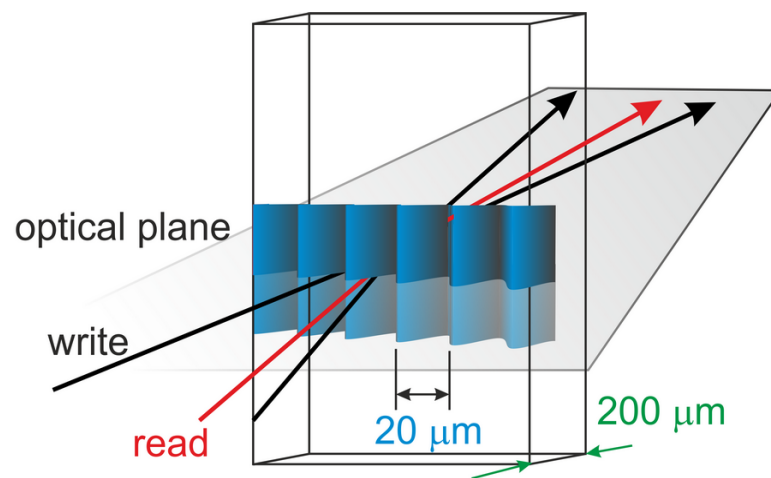
Charged colloidal rod with hairs



**Thermal diffusion
more sensitive to
the grafting of
the polymers**

... (more) projects in progress,

Measured quantity: Intensity of the diffracted beam



TDFRS Thermal diffusion forced Rayleigh scattering

homogeneous
temperature
and particle
distribution

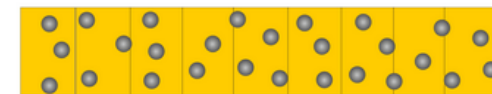
laser grating

temperature
grating

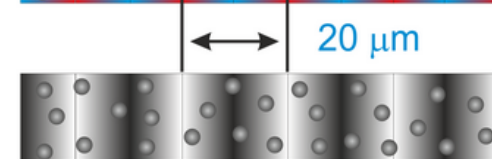
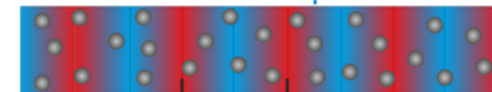
refractive index
grating

thermal diffusion

concentration
grating



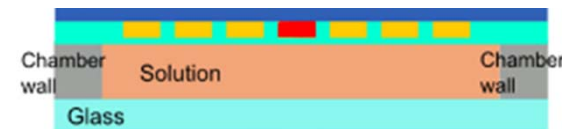
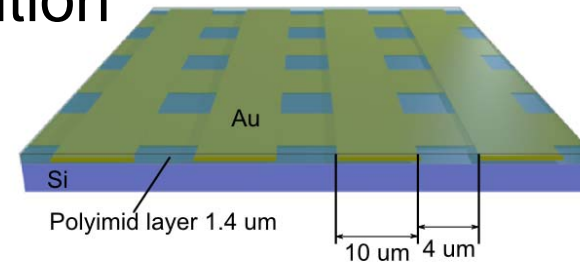
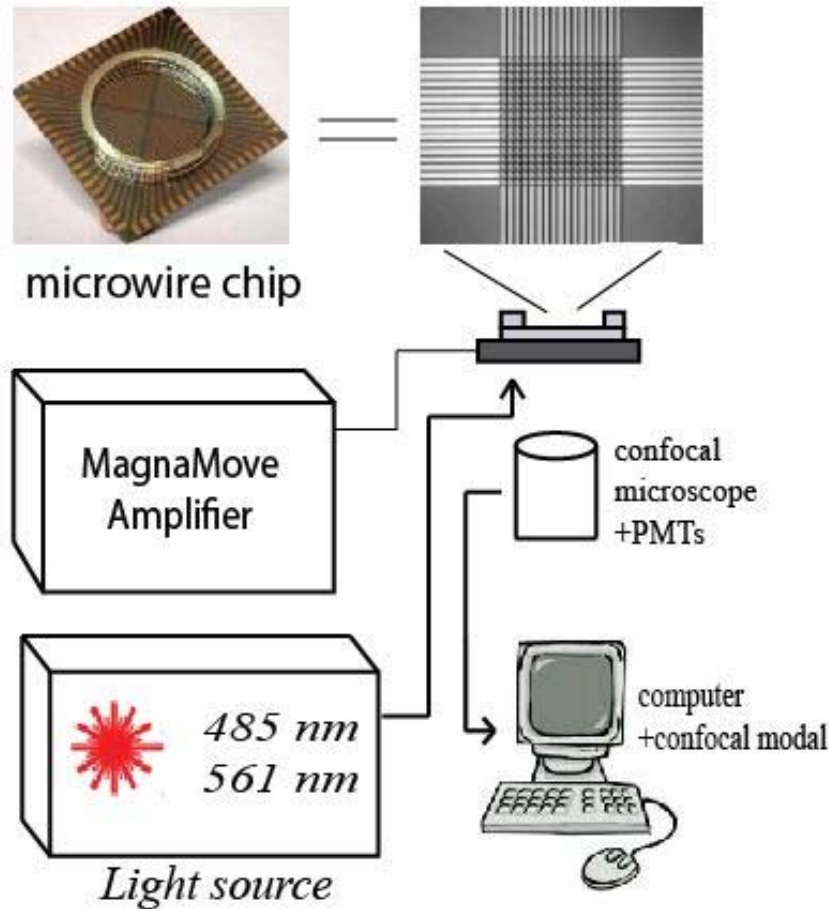
$$\Delta T = 20 - 100 \mu K$$



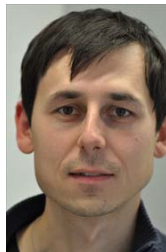
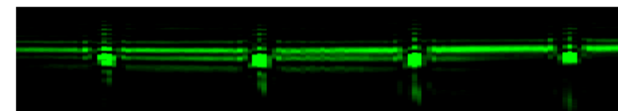
[S. Wiegand et al., J. Phys. Chem. B, **111**(2007) 14169]

Thermophoretic microfluidic cells microwire chip

Objective: investigation of
biomolecules in buffer
solution



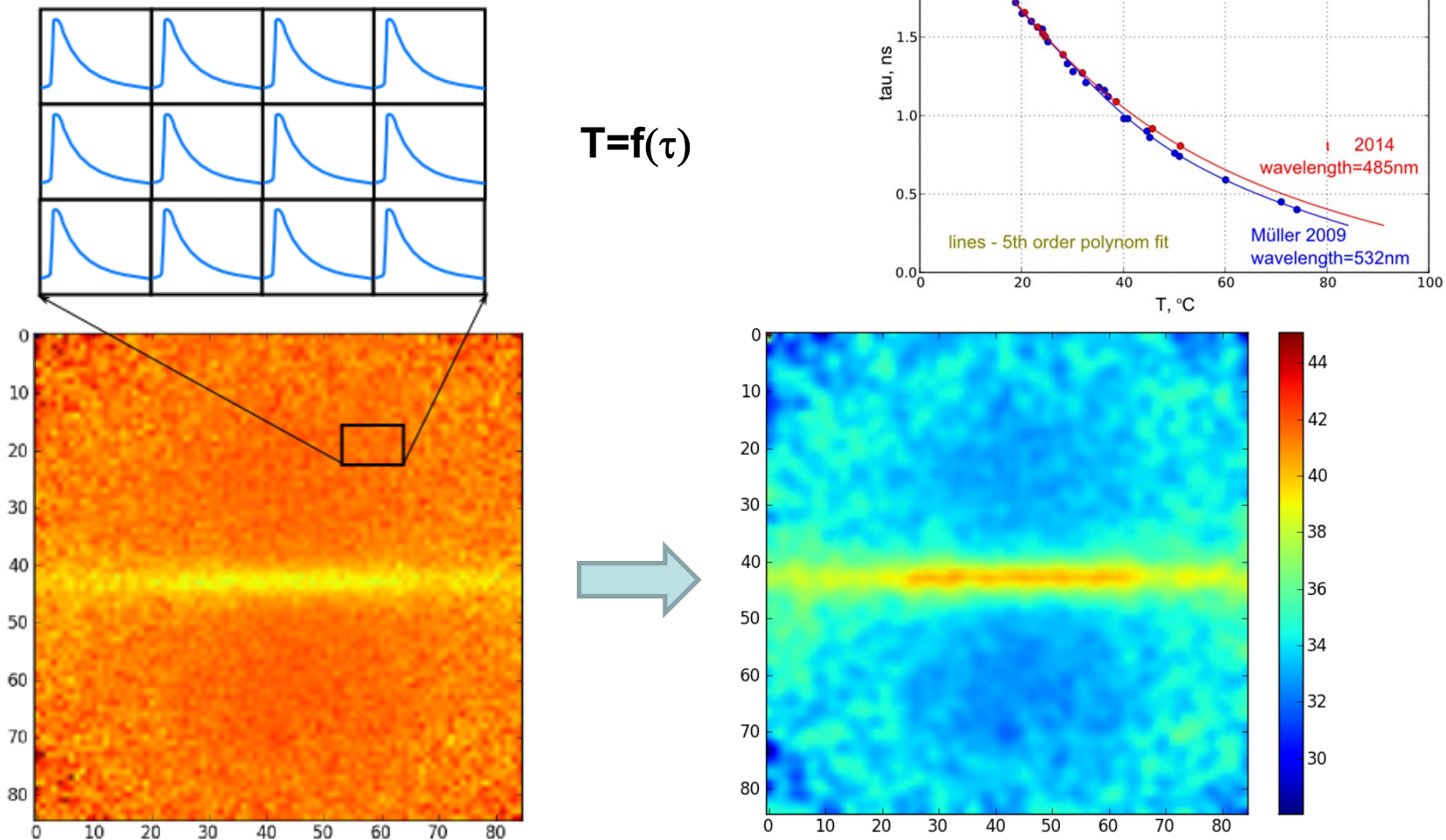
**Confocal XZ slice
(scattered light)**



[Rinklin, P., D. Afanasenkau, SW, A. Offenhäusser, and B. Wolfrum,
Lab on a Chip, 15 (2015) 237-243]

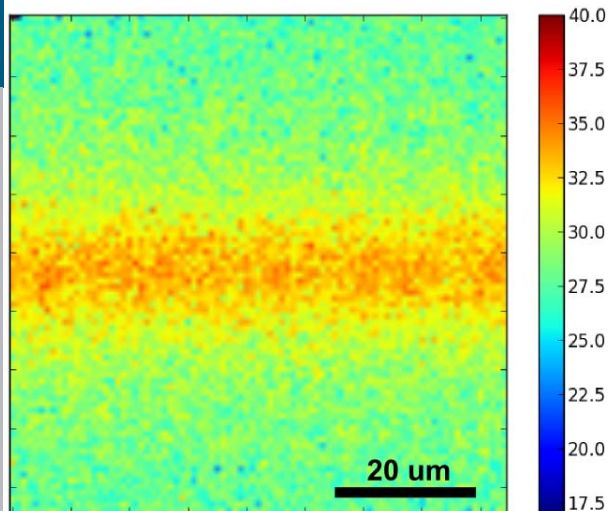
Thermophoretetic microfluidic cells

FLIM –
Fluorescence Life-time Imaging Microscopy

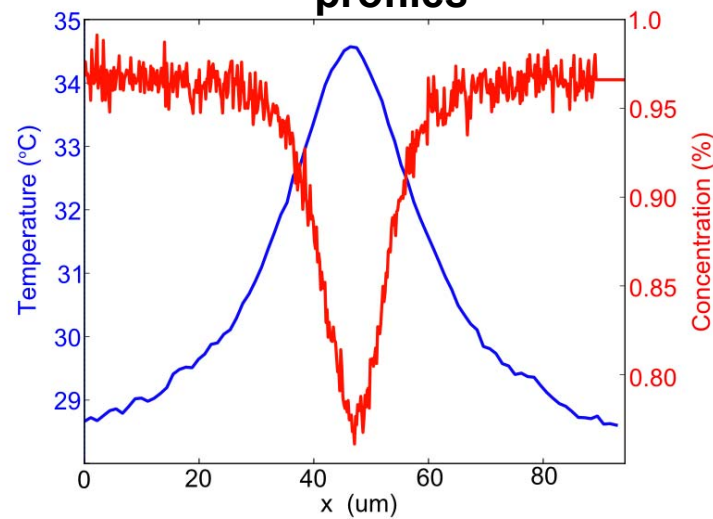


Thermophoretic microfluidic cells

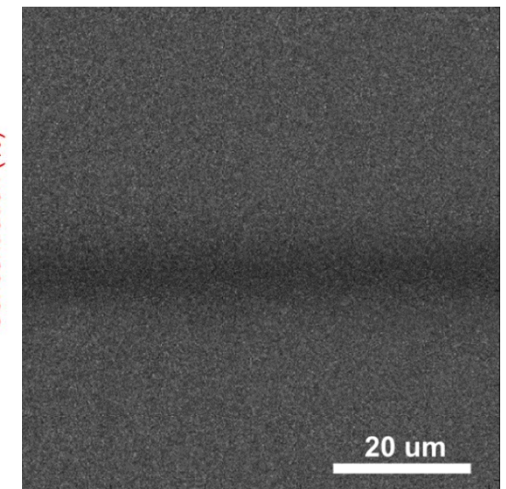
Temperature distribution



Temperature and concentration profiles

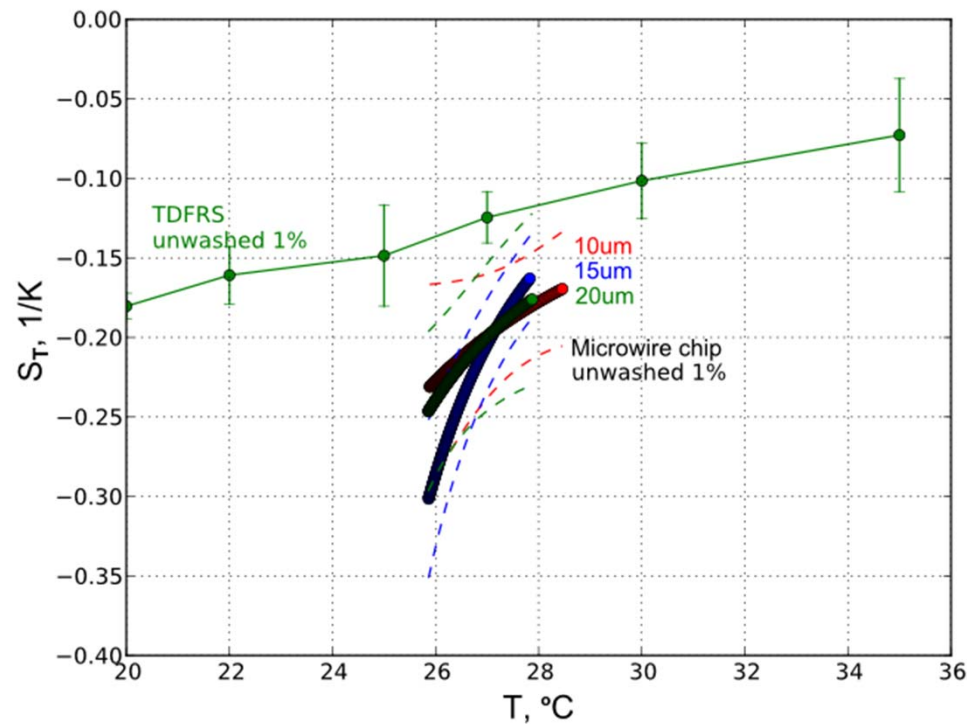


Intensity



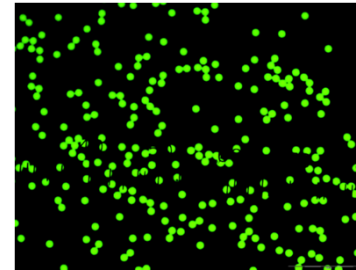
$$S_T = \frac{D}{D_T} = -\frac{1}{c} \frac{|\nabla c|}{|\nabla T|} = -\frac{1}{c} \frac{\left(\frac{dc}{dx}\right)}{\left(\frac{dT}{dx}\right)}$$

Preliminary thermophoresis results



System:

Fluoro-Max Dyed Green
Aqueous Fluorescent Particles
(G25) from Thermo Scientific



<http://www.thermoscientific.com>

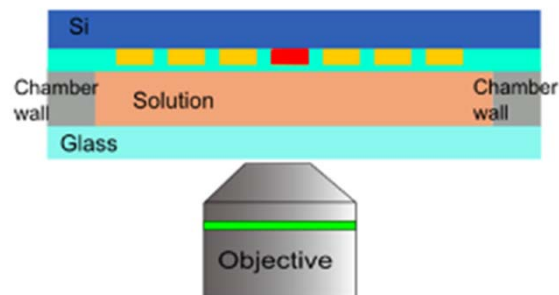
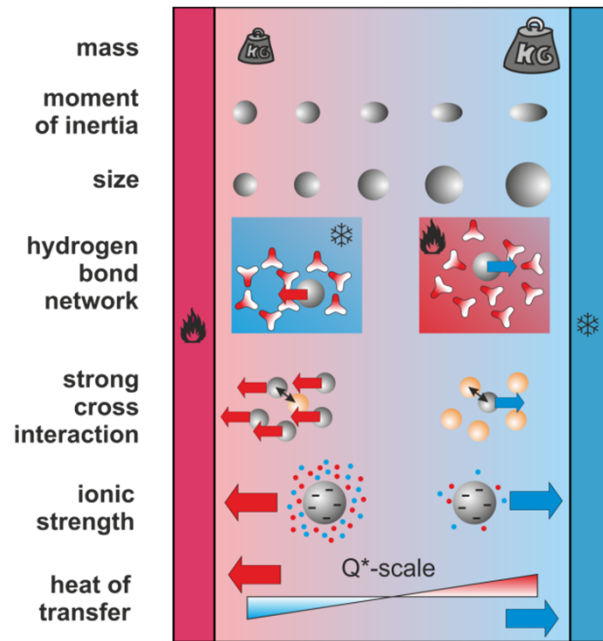
The surface of particles is carboxylated. Suspension contains traces of detergent and preservative agent.

SW1

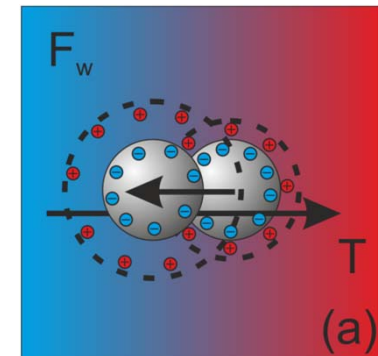
Technical problems

- Concentration changes
- Zero level
- Convection
- T measurements error ($\sim 20\%$)

Message to take home



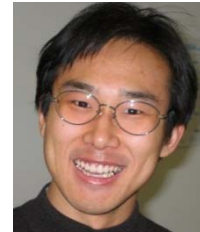
Thermophoresis
in aqueous
systems is
complex



Thank you for your attention and thanks to...



Jan Dhont –
support &
theory



Hui Ning –
Ludox particles



Zilin Wang –
fd virus



Johan Buitenhuis –
synthesis



Hartmut Kriegs -
technical support



Dzmitry
Afanasenkau -
thermophoretic
microfluidic cell

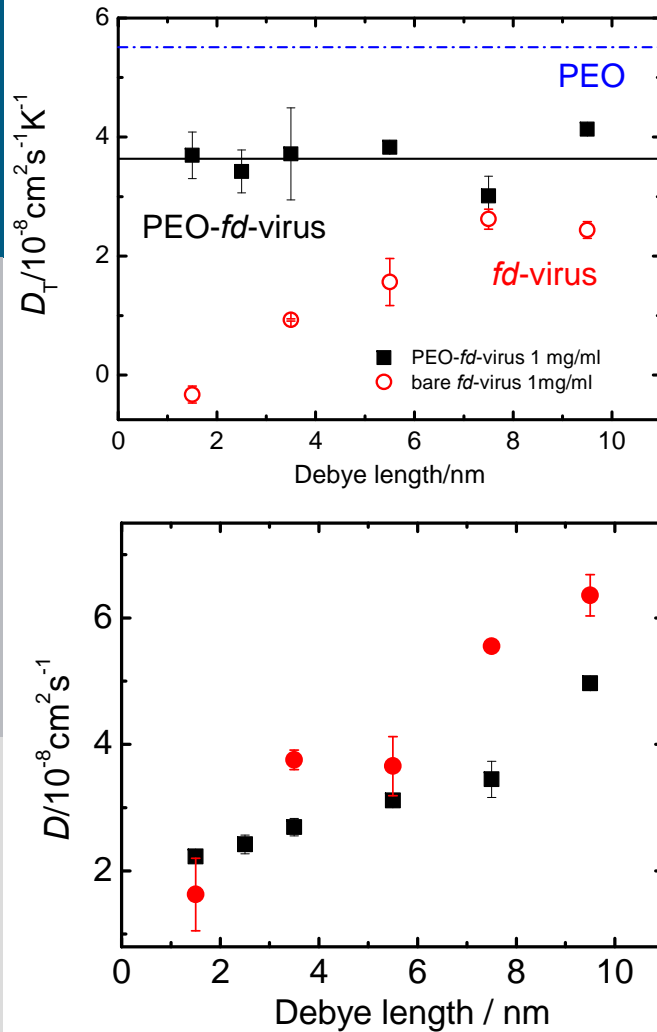


Bernhard Wolfrum –
Magma Move chip



Deutsche Forschungsgemeinschaft

Charged colloidal rod with hairs



Without hydrodynamic interactions:

$$D = \beta D_0 \frac{\partial \Pi}{\partial \rho}$$

$$\rho D_T = D_T^{theo} = \beta D_0 \frac{\partial \Pi}{\partial T}$$

.. Osmotic pressure

$$\Pi = \rho k_B T - \frac{2\pi}{3} \rho^2 \int_0^\infty dR R^3 \frac{dV^{DLVO}(R|T)}{dR} g(R|T)$$

$$D = D_0 [1 + 2B_2 \phi]$$

$$D_T = \frac{D_T^{theo}}{\rho} = \frac{D_0}{T} \left[1 + \frac{d(TB_2)}{dT} \phi \right]$$

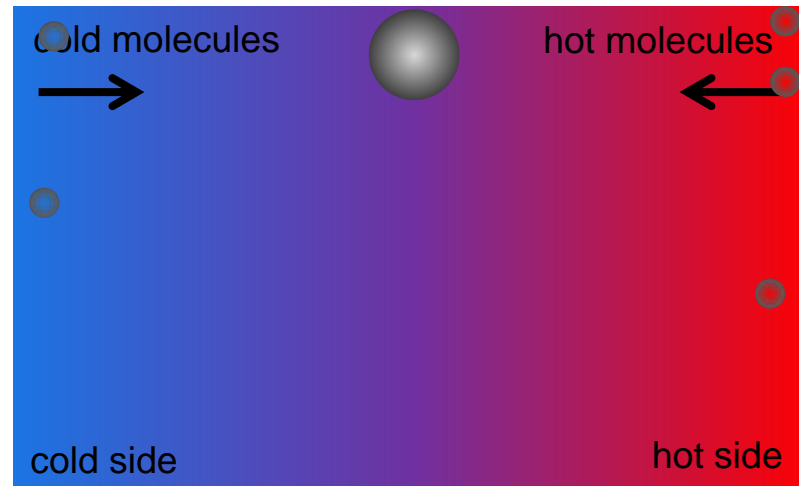
- Both **coefficients** show an increasing trend
- Magnitude is comparable

[Dhont, J.K.G., J. Chem. Phys., **120**(2004) 1632-1641]

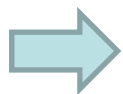


More theoretical work is required

Mass effect: animation



higher momentum transfer
from the warm side

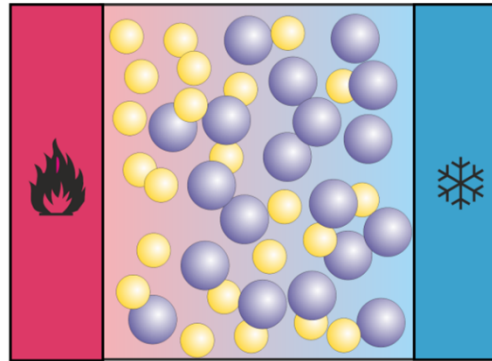
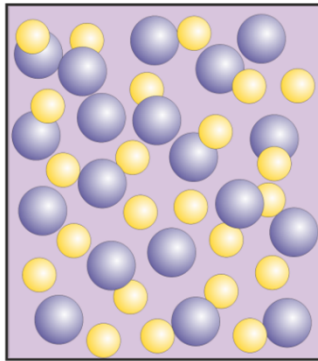


Enrichment of the heavy particles on the cold side

Phenomenological equation

(..., thermodiffusion, Soret effect) –

Movement of particles driven by a temperature gradient



$$\vec{j} = -D\vec{\nabla}c - c(1-c)D_T\vec{\nabla}T$$

Steady state $\vec{j}=0$

$$S_T = \frac{D_T}{D} \propto \frac{\Delta c}{\Delta T}$$

D - diffusion coefficient,

c - concentration,

D_T - thermodiffusion coefficient,

\vec{j} - flux, T – temperature

S_T – Soret coefficient

